## MODULE-4

## Chemical energetics

## SPONTANEITY OF CHEMICAL REACTIONS



We have studied about the first law of thermodynamics in lesson 11. According to this law the processes occur in such a way that the total energy of the universe remains constant. But it does not tell us whether a specified change or a process including a chemical reaction can occur spontaneously i.e., whether it is feasible or not. For example, the first law does not deny the possibility that a metal bar having a uniform temperature can spontaneously become warmer at one end and cooler at the other. But it is known from experience that such a change does not occur without expenditure of energy from an external source.

The first law also states that energy can be converted from one form into an equivalent amount of energy of another form. But it does not tell that heat energy cannot be completely converted into an equivalent amount of work without producing some changes elsewhere. In this lesson you shall learn to predict whether a given process or a chemical reaction can occur spontaneously or not.

## Objectives

After reading this lesson you will be able to :

- define entropy;
- recognise that entropy change in a system is given by

$$
\Delta \mathrm{S}=\frac{q_{\mathrm{rev}}}{T}
$$

- state entropy criterion for a spontaneous process $\Delta \mathrm{S}_{\text {universe }}>0$ and at equilibrium $\Delta S_{\text {universe }}=0$
- state third law of thermodynamics;
- state the relationship between G, H and S ;
- derive the relation $\Delta \mathrm{G}_{\text {system }}=\mathrm{T} \Delta \mathrm{S}_{\text {system }}$;

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- state Gibbs energy criterion for spontaneous process
$\Delta \mathrm{G}<0$ for a spontaneous process
$\Delta \mathrm{G}=0$ at equilibrium
$\Delta \mathrm{G}>0$ for a non-spontaneous process
- define standard Gibbs energy of formation of a subtance;
- relate the standard Gibbs energy change with the equilibrium constant and
- solve numerical problems.


### 12.1 Spontaneous and Non-spontaneous Processes

We know that hot water kept in a container cools down by losing heat to the surroundings. On the other hand, water at room temperature cannot become hot by gaining heat from the surroundings. It can be made hot by heating it over a gas burner. The cooling down of hot water is an example of a spontanneous process. Heating of water (at room temperature) is an example of a non-spontaneous process because an outside agency (gas burner) has been used.

A spontaneous process is a process that occurs in a system by itself; once started, no action from outside the system (outside agency) is necessary to make the process continue. A non-spontaneous process will not take place unless some external action is continuously applied. Let us consider another example, we know that when iron objects are exposed to moist atmosphere, rusting of iron takes place. Although the rusting of iron is a slow process but it always takes place in the same direction. We say that the rusting of iron is a spontaneous process. During rusting of iron, iron is oxidised to iron (III) oxide.

$$
4 \mathrm{Fe}(\mathrm{~s})+3 \mathrm{O}_{2}(\mathrm{~g}) \longrightarrow 2 \mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s})
$$

The reverse of the above reaction is also possible but it is non-spontaneous. An external agency has to be used to reduce iron (III) oxide to iron.
From our discussion it can be concluded that

- if a process is spontaneous, the reverse process is non-spontaneous.
- both spontaneous and non-spontaneous processes are possible.
- spontaneous processes occur naturally whereas non-spontaneous processes require the help of an outside agency to occur.


### 12.2 Entropy

In fig 12.1(a) the bulb 'I' contains 1 mol of an ideal gas ' A ' at a pressure of 1 bar and the bulb II contains 1 mol of another ideal gas ' B ' at 1 bar. The two bulbs are joined together through a valve.


Fig 12.1

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When the valve between the two bulbs is opened [Fig 12.1 (b)], the two gases mix spontaneously. The mixing of gases continues until the partial pressure of each gas becomes equal to 0.5 bar in each bulb i.e., the equilibrium is attained. We know from experience that the process cannot be reversed spontaneously - the gases do not unmix. What is the driving force behind this process?

We know that the internal energy $(U)$ and enthalpy $(H)$ of an ideal gas depend only upon the temperature of the gas and not upon its pressure or volume. Since there are no intermolecular forces in ideal gases, $\Delta U=\Delta H=0$ when ideal gases mix at constant temperature. Thus energy change is not the driving force behind the spontaneous mixing of ideal gases. The driving force is simply the tendency of the molecules of the two gases to achieve maximum state of mixing, i.e., disorder. The thermodynamic property related to the disorder of the system is called entropy. It is denoted by the symbol $S$.

The entropy is the measure of disorder or randomness in a system. The greater the disorder in a system, the greater is the entropy of the system.

For a given substance,
(i) the crystalline state is the most ordered state, hence its entropy is the lowest.
(ii) the gaseous state is the most disordered state, hence its entropy is the maximum, and (iii) the disorder in the liquid state is intermediate between the solid and the gaseous state. When a system changes from one state to another, the change of entropy $\Delta S$ is given by

$$
\begin{equation*}
\Delta S=\frac{q_{\mathrm{rev}}}{T} \tag{12.1}
\end{equation*}
$$

where $q_{\text {rev }}$ is the heat supplied reversibly at temperature $T$.

### 12.3 Criteria for Spontaneous Change : <br> The Second Law of Thermodynamics

So far we have studied about internal energy, enthalpy and entropy. Can we define the spontaneity of a process in terms of these properties? Let us see whether these changes in properties can be used as a criterion for determining the spontaneity of a process or not.
(i) We know that most of the processes which occur spontaneously are exothermic. Water kept in a container at room temperature evaporates spontaneously. It is an endothermic process. Thus enthalpy change cannot be used as a criteria for spontaneous change.
(ii) Can we use the increase of entropy as a criteria for the spontaneous change? Then how do we explain the spontaneous freezing of water at $-10^{\circ} \mathrm{C}$ ? We know that crystalline ice is more ordered then the liquid water and therefore the entropy must decrease. The answer to this question is that we must consider simultaneously two entropy changes:
(a) the entropy change of the system itself, and
(b) the entropy change of the surroundings


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$$
\begin{equation*}
\Delta S_{\text {total }}=\Delta S_{\text {univ }}=\Delta S_{\text {system }}+\Delta S_{\text {surroundings }}>0 \tag{12.2}
\end{equation*}
$$

The equation is one of the many forms of the second law of thermodynamics.
According to the second law of thermodynamics all spontaneous or natural processes produce an increase in entropy of the universe.

Thus, for a spontaneous process when a system is at equilibrium, the entropy is at maximum, and the change in entropy is zero

$$
\begin{equation*}
\Delta S=0 \text { (at equilibrium) } \tag{12.3}
\end{equation*}
$$

### 12.4 Entropy Change in Phase Transitions

When a solid melts and produces liquid, the process occurs at the melting point of the solid. For example, ice melts at 273 K and produces water at the same temperature.

$$
\mathrm{H}_{2} \mathrm{O}(\mathrm{~s}) \xrightarrow{\text { at } 273 \mathrm{~K}} \mathrm{H}_{2} \mathrm{O}(l)
$$

The heat involved in the process of melting is called enthalpy of fusion $\left(\Delta_{\text {fus }} H\right)$. Therefore, the entropy of fusion ( $\Delta_{\text {fus }} S$ ) is given by

$$
\Delta_{\text {fus }} S=\frac{\Delta_{\mathrm{fus}} H}{T}\left(\because q_{\mathrm{rev}} \text { at const } p=\Delta_{\text {fus }} H\right)
$$

Similarly, for the equilibrium

$$
\begin{aligned}
& \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \xrightarrow{\text { at } 373 \mathrm{~K}} \mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \\
& \Delta_{\text {vap }} S=\frac{\Delta_{\text {vap }} H}{T},(\mathrm{~T} \text { is the boiling point })
\end{aligned}
$$

Example 12.1: The enthalpy change for the transition of liquid water to steam at 373 K is $40.8 \mathrm{~kJ} \mathrm{~mol}^{-1}$. Calculate the entropy change for the process

Solution: $\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \stackrel{373 \mathrm{~K}}{\rightleftharpoons} \mathrm{H}_{2} \mathrm{O}(\mathrm{g})$

$$
\begin{aligned}
& \Delta_{\text {vap }} S=\frac{\Delta_{\text {vap }} H}{T} \\
& \Delta_{\text {vap }} H=40.8 \mathrm{~kJ} \mathrm{~mol}^{-1}=40.8 \times 10^{3} \mathrm{~J} \mathrm{~mol}^{-1} \\
& \mathrm{~T}=373 \mathrm{~K}
\end{aligned}
$$

$$
\Delta_{\text {vap }} S=\frac{40.8 \times 10^{3} \mathrm{~J} \mathrm{~mol}^{-1}}{373 \mathrm{~K}}=109 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}
$$

## Intext Questions 12.1

1. The enthalpy change for the transition of ice to liquid water at 273 K is 6.02 kJ $\mathrm{mol}^{-1}$. Calculate the entropy change for the process.
2. Arrange the following systems in the order of increasing randomness,
(i) 1 mol of gas A
(ii) 1 mol of solid A
(iii) 1 mol of liquid A
3. Indicate whether you would expect the entropy of the system to increase or decrease
(a) $2 \mathrm{SO}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{SO}_{3}(\mathrm{~g})$
(b) $\mathrm{N}_{2}(\mathrm{~g})+3 \mathrm{H}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{NH}_{3}(\mathrm{~g})$
(c) $\mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{O}(\mathrm{g})$

### 12.5 Absolute Entropy

When the temperature of a substance is increased, the translational, vibrational and rotational motions become more vigorous. It leads to greater disorder and as a result the entropy of the substance increases. Thus, on increasing the temperature of a substance the entropy of a substance increases. It decreases on decreasing the temperature of a substance.

According to Walther Nernst, the entropy of a pure perfectly crystalline substance approaches zero as the temperature approaches absolute zero. This is known as the Third law of thermodynamics. This third law of thermodynamics helps us to calculate the absolute value of molar entropies $\left(S_{\mathrm{m}}\right)$ of substances at different temperatures. The standard molar entropies of some substances at 298 K are given in Table 12.1.

Table 12.1 : Standard molar entropies ( $S_{\mathrm{m}}{ }^{\mathbf{}} / \mathrm{J} \mathrm{K}^{-1} \mathrm{~mol}^{-1}$ ) at 298 K

| Solids | Entropy | Liquids | Entropy | Gases | Entropy |
| :--- | :--- | :--- | :--- | :--- | :--- |
| C (graphite) | 5.7 | $\mathrm{H}_{2} \mathrm{O}$ | 69.9 |  |  |
| C (diamond) | 2.4 | Hg | 76.0 |  |  |
| Fe | 27.3 | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}$ | 160.7 |  |  |
| Pb | 64.8 | $\mathrm{C}_{6} \mathrm{H}_{6}$ | 173.3 |  |  |
| Cu | 33.1 | $\mathrm{CH}_{3} \mathrm{COOH}$ | 159.8 |  |  |
| Al | 96.2 |  |  |  |  |
| $\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}$ | 360.8 |  |  |  |  |
| $\mathrm{CaCO}_{3}$ | 92.9 |  |  | 130.7 |  |
| $\mathrm{O}_{2}$ | 195.1 |  |  |  |  |
| $\mathrm{~N}_{2}$ | 191.6 |  |  |  |  |
| $\mathrm{CO}_{2}$ | 213.7 |  |  |  |  |
| $\mathrm{NO}_{2}$ | 240.1 |  |  |  |  |
| $\mathrm{~N}_{2} \mathrm{O}_{4}$ | 304.3 |  |  |  |  |
| $\mathrm{NH}_{3}$ | 192.3 |  |  |  |  |
| $\mathrm{CH}_{4}$ | 186.2 |  |  |  |  |

## Entropy Change for a Reaction

The absolute entropies can be used for calculating standard entropies changes accompanying chemical reaction. It can be determined by subtracting the standard entropies of reactants from those of products. Thus, for a general reaction

$$
\mathrm{aA}+\mathrm{bB}+\ldots \ldots \rightarrow \mathrm{pP}+\mathrm{qQ}+\ldots
$$



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$$
\begin{aligned}
& \Delta S_{\mathrm{m}}{ }^{0}=\left[\mathrm{p} S_{\mathrm{m}}{ }^{0}(\mathrm{P})+\mathrm{q} S_{\mathrm{m}}{ }^{0}(\mathrm{Q})+\ldots .\right]-\left[\mathrm{a} S_{\mathrm{m}}{ }^{0}(\mathrm{~A})+\mathrm{b} S_{\mathrm{m}}{ }^{0}(\mathrm{~B})+\ldots\right] \\
& \Delta_{r} S_{\mathrm{m}}{ }^{0}=\Sigma S_{\mathrm{m}}{ }^{0}(\text { products })-\Sigma S_{\mathrm{m}}{ }^{0}(\text { reactants })
\end{aligned}
$$

Example 12.2: Calculate the entropy change, $\Delta_{\mathrm{r}} \mathrm{S}_{\mathrm{m}}{ }^{0}$ for the following reaction at 298 K .
$4 \mathrm{Fe}(\mathrm{s})+3 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s})$
Given that the standard molar entropies of $\mathrm{Fe}(\mathrm{s}), \mathrm{O}_{2}(\mathrm{~g})$, and $\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s})$ at 298 K are 27.3, 205.0 and $87.4 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$ respectively.

Solution : $4 \mathrm{Fe}(\mathrm{s})+3 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s})$
$\Delta_{\mathrm{r}} S^{\mathrm{o}}=\sum v_{\mathrm{P}} S_{\mathrm{m}}^{\mathrm{o}}$ (products) $-\sum v_{\mathrm{R}} S^{\mathrm{o}}{ }_{\mathrm{m}}$ (reactants)
$\Delta_{\mathrm{r}} S^{\mathrm{o}}=2 S_{\mathrm{m}}^{\mathrm{o}}\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)-\left[4 S_{\mathrm{m}}^{\mathrm{o}}(\mathrm{Fe})+3 S_{\mathrm{m}}^{\mathrm{o}}\left(\mathrm{O}_{2}\right)\right]$
$=[2 \times 87.4-(4 \times 27.3+3 \times 205.0)] \mathrm{J} \mathrm{K}^{-1} \mathrm{~mol}^{-1}$
$=-549.4 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$

### 12.6 Gibbs Energy and Spontaneity

We can use the expression

$$
\begin{equation*}
\Delta S_{\text {univ }}=\Delta S_{\text {total }}=\Delta S_{\text {system }}+\Delta S_{\text {surrounding }}>0 \tag{12.4}
\end{equation*}
$$

as our basic criterion for a spontaneous change. But it is very difficult to apply it because we have to evaluate the total entropy change i.e. the entropy change of system plus that of surroundings. This is a tedious process as it is difficult to figure out all the interactions between the system and the surroundings. Thus, for a system which is not isolated from its surroundings.

$$
\begin{equation*}
\Delta S_{\text {total }}=\Delta S_{\text {system }}+\Delta S_{\text {surrounding }} \tag{12.5}
\end{equation*}
$$

At constant temperature and pressure if $q_{\mathrm{p}}$ is the heat given out by the system to the surroundings, we can write

$$
\begin{equation*}
\Delta S_{\text {surrounding }}=\frac{-q_{p}}{T}=-\frac{\Delta H_{\text {system }}}{T} \tag{12.6}
\end{equation*}
$$

(since $q_{\mathrm{p}}=\Delta H$ at constant pressure)
Substituting Eq. 12.6 in Eq. 12.5, we get

$$
\begin{gather*}
\Delta S_{\text {total }}=\Delta S_{\text {system }}-\frac{\Delta H_{\text {system }}}{T} \\
\mathrm{~T} \Delta S_{\text {total }}=\mathrm{T} \Delta S_{\text {system }}-\Delta H_{\text {system }} \\
\text { or }-\mathrm{T} \Delta S_{\text {total }}=\Delta H_{\text {system }}-\mathrm{T} \Delta S_{\text {system }} \tag{12.7}
\end{gather*}
$$

Now, let us define another thermodynamic property, Gibbs energy. It is defined by the equation

$$
\begin{equation*}
G=H-T S \tag{12.8}
\end{equation*}
$$

For a change in Gibbs energy, we write

$$
\begin{aligned}
& \Delta G=\Delta H-\Delta(T S) \\
& \Delta G=\Delta H-T \Delta S-S \Delta T
\end{aligned}
$$

For a change at constant temperature, $\Delta T=0$,
Therefore $\quad \Delta G=\Delta H-T \Delta S$
Since $H, T$ and $S$ are state functions, it follows that $G$ is also a state function. Comparing equations 12.7 and 12.9 , we find that

$$
\begin{equation*}
\Delta G=-T \Delta S_{\text {Total }} \tag{12.10}
\end{equation*}
$$

We have seen that if $\Delta S_{\text {Total }}$ is positive, the change will be spontaneous. Equations 12.10 can be used to predict the spontaneity of a process based on the value of $\Delta G$.
The use of Gibbs energy has the advantage that it refers to system only. Thus for a process occurring at constant temperature and pressure, if
$\Delta G<0$ (negative), the process is spontaneous
$\Delta G>0$ (positive), the process is non-spontaneous
$\Delta G=0$ (zero), the process is at equilibrium
In deciding the spontaneity of a chemical reaction, the equation $\Delta G=\Delta H-T \Delta S$ takes into account two factors (i) the energy factor $\Delta H$, and (ii) the entropy factor $\Delta S$. Based on the signs of $\Delta H$ and $\Delta S$ there are four possibilities for $\Delta G$. These possibilities are outlined in table 12.2

Table 12.2 Criterion for spontaneous change : $\Delta \boldsymbol{G}=\Delta \boldsymbol{H}-\boldsymbol{T} \Delta S$

| S.No | $\Delta H$ | $\Delta S$ | $\Delta G$ | Result |
| :--- | :--- | :--- | :--- | :--- |
| 1 | - | + | - | Spontaneous at all temperatures. |
| 2. | - | - | - | Spontaneous at low temperatures. |
|  |  |  | + | Non-spontaneous at high temperatures. |
| 3. | + | + | + | Non-spontaneous at low temperatures. |
|  |  |  | - | Spontaneous at high temperatures. |
| 4. | + | - | + | Non-spontaneous at all temperatures. |

Example 12.3: For the reaction

$$
2 \mathrm{NO}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{NO}_{2}(\mathrm{~g})
$$

Calculate $\Delta_{r} G$ at 700 K when enthalpy and entropy changes ( $\Delta_{\mathrm{r}} H$ and $\Delta_{\mathrm{r}} S$ ) are respectively $-113.0 \mathrm{~kJ} \mathrm{~mol}^{-1}$ and $-145 \mathrm{JK}^{-1} \mathrm{~mol}^{-1}$

Solution : Given that

$$
\begin{aligned}
& \Delta H=-113.0 \mathrm{~kJ} \mathrm{~mol}^{-1} \\
& \Delta S=-145 \mathrm{JK}^{-1} \mathrm{~mol}^{-1}=-145 \times 10^{-3} \mathrm{~kJ} \mathrm{~K}^{-1} \mathrm{~mol}^{-1} \\
& T=700 \mathrm{~K}
\end{aligned}
$$

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Substituting the values in

$$
\begin{aligned}
& \Delta G=\Delta H-T \Delta S \\
& \Delta G=\left(-113.0 \mathrm{~kJ} \mathrm{~mol}^{-1}\right)-(700 \mathrm{~K})\left(-145 \times 10^{-3} \mathrm{~kJ} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}\right) \\
& =\left(-113.0 \mathrm{~kJ} \mathrm{~mol}^{-1}\right)+\left(101.5 \mathrm{~kJ} \mathrm{~mol}^{-1}\right) \\
& =-11.5 \mathrm{~kJ} \mathrm{~mol}^{-1}
\end{aligned}
$$

## Intext Questions 12.2

1. Determine whether the following reaction
$\mathrm{CCl}_{4}(\mathrm{l})+\mathrm{H}_{2}(\mathrm{~g}) \rightarrow \mathrm{HCl}(\mathrm{g})+\mathrm{CHCl}_{3}(\mathrm{l})$
is spontaneous at 298 K if $\Delta_{\mathrm{r}} \mathrm{H}=91.35 \mathrm{~kJ} \mathrm{~mol}^{-1}$ and $\Delta_{\mathrm{r}} S=41.5 \mathrm{JK}^{-1} \mathrm{~mol}^{-1}$ for this reaction.
2. Which of the following conditions would predict a process that is always spontaneous?
(i) $\Delta H>0, \Delta S>0$
(ii) $\Delta H>0, \Delta S<0$
(iii) $\Delta H\langle 0, \Delta S\rangle 0$
(iv) $\Delta H<0, \Delta S<0$

### 12.7 Standard Gibbs Energy Change ( $\Delta \mathbf{G}^{\mathbf{0}}$ ) and Equilibrium Constant (K)

The standard Gibbs energy change is defined as the change in Gibbs energy for the process in which the reactants in their standard states are converted into the products in their standard states. It is denoted by the symbol $\Delta_{\mathrm{r}} \mathrm{G}^{\circ}$.

The value of $\Delta_{r} G^{\circ}$ can be found from the standard Gibbs energy of formation of substances.
The standard Gibbs energy of formation of a compound is defined as the change in Gibbs energy when 1 mole of the compound is formed from its constituent elements in their standard states. Like the standard enthalpy of formation of an element, the standard Gibbs energy of formation of an element in its standard state is taken as zero.

Thus for a reaction

$$
\begin{aligned}
& \mathrm{aA}+\mathrm{bB}+\ldots . \rightarrow \mathrm{pP}+\mathrm{qQ}+\ldots \\
& \Delta_{\mathrm{r}} G^{\circ}=\left(\mathrm{p} \Delta_{\mathrm{f}} G_{\mathrm{P}}^{\mathrm{o}}+\mathrm{q} \Delta_{\mathrm{f}} G_{\mathrm{Q}}^{\mathrm{o}}+\ldots .\right)-\left(\mathrm{a} \Delta_{\mathrm{f}} G_{\mathrm{A}}^{\mathrm{o}}+\mathrm{b} \Delta_{\mathrm{f}} G_{\mathrm{B}}^{\mathrm{o}}+\ldots .\right) \\
& \Delta_{\mathrm{r}} G^{\circ}=\sum \Delta_{\mathrm{f}} G^{\circ}(\text { products })-\sum \Delta_{f} G^{\circ} \text { (reactants) }
\end{aligned}
$$

The standard Gibbs energy change ( $\Delta_{\mathrm{r}} G^{\circ}$ ) is related to the equilibrium constant (K) of the reaction by the expression

$$
\Delta_{\mathrm{r}} G^{\mathrm{o}}=-R T \ln K=-2.303 R T \log K
$$

Example 12.4: The equilibrium constant of the reaction

$$
P(\mathrm{~s})+\frac{3}{2} \mathrm{Cl}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{PCl}_{3}(\mathrm{~g})
$$

is $2.00 \times 10^{24}$ at 500 K . Calculate the value of $\Delta_{\mathrm{r}} G^{\circ}$.
Solution : Given that

$$
\begin{aligned}
& K= 2.00 \times 10^{24} \\
& T= 500 \mathrm{~K} \\
& \begin{aligned}
\Delta_{\mathrm{r}} G^{\circ} & =-2.303 R T \log K \\
& =-2.303 \times\left(8.314 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}\right)(500 \mathrm{~K}) \log 2.0 \times 10^{24} \\
& =-2.303 \times\left(8.314 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}\right)(500 \mathrm{~K}) 24.30 \\
& =-232.6 \mathrm{~kJ} \mathrm{~mol}^{-1}
\end{aligned}
\end{aligned}
$$

Example 12.5 : Calculate the standard Gibbs energy change for the reaction

$$
\mathrm{CH}_{4}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \longrightarrow \mathrm{CO}_{2}(\mathrm{~g})+2 \mathrm{H}_{2} \mathrm{O} \text { (l) }
$$

at 298 K . The standard Gibbs energies of formation of $\mathrm{CH}_{4}, \mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$ at 298 K are $-50.8 \mathrm{~kJ} \mathrm{~mol}^{-1}$, $-394.4 \mathrm{~kJ} \mathrm{~mol}^{-1}$, and $-237.2 \mathrm{~kJ} \mathrm{~mol}^{-1}$ respectively.

Solution : $\mathrm{CH}_{4}(\mathrm{~g})+2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{CO}_{2}(\mathrm{~g})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l})$

$$
\begin{aligned}
\Delta_{\mathrm{r}} G^{\circ} & =\Delta_{\mathrm{f}} G^{\circ}\left(\mathrm{CO}_{2}\right)+2 \Delta_{\mathrm{f}} \mathrm{G}^{\circ}\left(\mathrm{H}_{2} \mathrm{O}\right)-\Delta_{\mathrm{f}} \mathrm{G}^{\circ}\left(\mathrm{CH}_{4}\right)-2 \Delta_{\mathrm{f}} G^{\circ}\left(\mathrm{O}_{2}\right) \\
& =-394.4+2 \times(-237.2)-(-50.8)-2 \times 0 \\
& =-394.4-474.4+50.8 \\
& =-818 \mathrm{~kJ} \mathrm{~mol}^{-1}
\end{aligned}
$$

## Intext Questions 12.3

1. What is the relationship between the standard Gibbs energy change and the equilibrium constant of the reaction?
$\qquad$
2. The standard Gibbs energy change for the reaction
$\mathrm{CO}(\mathrm{g})+2 \mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{CH}_{3} \mathrm{OH}(\mathrm{l})$
at $298 \mathrm{~K}^{\text {is }}-24.8 \mathrm{~kJ} \mathrm{~mol}^{-1}$. What is the value of the equilibrium constant at 298 K ?

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## What You Have Learnt

- All spontaneous processes lead to an increase in disorder or randomness
- The thermodynamic function related to disorder in a system is called entropy, $S$.
- For a spontaneous change the total entropy change of the system and the surroundings must increase.
- Gibbs energy is defined as $G=H-T S$
- At a constant temperature, the change in Gibbs free energy is related to enthalpy and entropy changes by the expression

$$
\Delta G=\Delta H-T \Delta S
$$

For a spontaneous change, there must be a decrease in Gibbs energy, i.e., $\Delta G<0$.
At equilibrium $\Delta G=0$
The standard Gibbs energy change is related to the equilibrium constant of the reaction by the expression

$$
\Delta_{\mathrm{r}} G^{\circ}=-2.303 R T \log K
$$

- The standard Gibb's energy change is given by

$$
\Delta_{r} G^{\circ}=\sum \Delta_{\mathrm{f}} G^{0} \text { (products) }-\sum \Delta_{\mathrm{f}} G^{0} \text { (reactants) }
$$



## Terminal Exercise

1. What do you call the measure of disorder or randomness in a system?
2. Predict the sign of $\Delta S$ for each of the following processes.
(i) $\mathrm{H}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{H}(\mathrm{g})$
(ii) $\mathrm{O}_{2}(\mathrm{~g}, 300 \mathrm{~K}) \rightarrow \mathrm{O}_{2}(\mathrm{~g}, 500 \mathrm{~K})$
3. Define entropy.
4. Explain why entropy is not a good criteria for determining the spontaneity of a process?
5. What is the relationship between the enthalpy and the entropy change for a system at equilibrium?
6. For the reaction
$\mathrm{O}_{3}(\mathrm{~g})+\mathrm{O}(\mathrm{g}) \rightarrow 2 \mathrm{O}_{2}(\mathrm{~g})$
$\Delta_{r} H=-391.9 \mathrm{~kJ} \mathrm{~mol}^{-1}$ and $\Delta_{r} S=10.3 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$ at 298 K . Calculate $\Delta_{r} G$ at this temperature and state whether the reaction is spontaneous or not.
7. What happens to $\Delta_{r} G$ during
(a) a spontaneous process
(b) a non-spontaneous process
(c) a process at equilibrium
8. Calculate $\Delta_{r} G^{\circ}$ at 298 K for the reaction
$2 \mathrm{NO}_{2}(\mathrm{~g}) \rightarrow \mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g})$
Given $\Delta_{r} H=-57.20 \mathrm{~kJ} \mathrm{~mol}^{-1}$ and $\Delta_{r} S=-175.8 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$
Is this reaction spontaneous?
9. The standard Gibbs energies of formation at 298 K are $-202.85 \mathrm{~kJ} \mathrm{~mol}^{-1}$ for $\mathrm{NH}_{4} \mathrm{Cl}(\mathrm{s}),-16.45 \mathrm{~kJ} \mathrm{~mol}^{-1}$ for $\mathrm{NH}_{3}(\mathrm{~g})$ and $-95.3 \mathrm{~kJ} \mathrm{~mol}^{-1}$ for $\mathrm{HCl}(\mathrm{g})$
(a) What is $\Delta_{r} G^{\circ}$ for the reaction
$\mathrm{NH}_{4} \mathrm{Cl}(\mathrm{s}) \rightleftharpoons \mathrm{NH}_{3}(\mathrm{~g})+\mathrm{HCl}(\mathrm{g})$
(b) Calculate the equilibrium constant for this decomposition.
10. For the following reaction
$\mathrm{CCl}_{4}(\mathrm{l})+\mathrm{H}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{HCl}(\mathrm{g})+\mathrm{CHCl}_{3}(\mathrm{l})$
$\Delta_{r} G^{\circ}=-103.7 \mathrm{~kJ} \mathrm{~mol}^{-1}$ at 298 K . Calculate the equilibrium constant for this reaction.

## Answers to Intext Questions

12.1

1. $\Delta_{\text {fus }} S=\frac{\Delta_{\text {fus }} H}{T}=\frac{6.02 \mathrm{~kJ} \mathrm{~mol}^{-1}}{273 \mathrm{~K}}=\frac{6.02 \times 10^{3} \mathrm{~J} \mathrm{~mol}^{-1}}{273 \mathrm{~K}}$

$$
=22.0 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}
$$

2. 1 mol of solid, 1 mol of liquid, 1 mol of gas.
3. Decrease (b) Decrease (c) Increase

## 12.2

1. $\Delta \mathrm{G}=-103.7 \mathrm{~kJ}$. Therefer the reaction is spontaneous.
2. (iii)

## 12.3

1. $\Delta \mathrm{G}^{\mathrm{o}}=-2.303 \mathrm{RT} \log \mathrm{K}$
2. $2.2 \times 10^{4}$

# SENIOR SECONDARY COURSE <br> CHEMISTRY <br> Student's Assignment - 3 

## Maximum Marks: 50 <br> Time: $1 \frac{1}{2}$ Hours

## INSTRUCTIONS

- Answer all the questions on a separate sheet of paper.
- Give the following information on your answer sheet:
- Name
- Enrolment Number
- Subject
- Assignment Number
- Address
- Get your assignment checked by the subject teacher at your study centre so that you get positive feedback about your performance.


## Do not send your assignment to NIOS

1. (a) Give one example each of the following types of solutions :
(i) Liquid in solid
(ii) Solid in gas
(b) What is Brownian motion?
(c) Give one example each of the following types of colloids :
(i) Liquid in solid
(ii) Solid in gas
(d) Define enthalpy of formation of a compound.
(e) What are state functions? Give one example.
(f) Is enthalpy of reactants less or more than that of products in an endothermic reaction?
(g) Define entropy.
(h) What happens to the free energy of a system during a non-spontaneous process?
(i) What is the relationship between free energy change and equilibrium constant?
(j) Mention the relation between $\mathrm{K}_{\mathrm{p}}$ and $\mathrm{K}_{\mathrm{c}}$.
2. (a) What is an ideal solution? Give one example.
(b) What is a colligative property? Name two such properties.
(c) Distinguish between lyophilic and lyophobic colloids. Given one example of each.
(d) What are the causes of charge on colloidal particles?
(e) What is a (i) closed system (ii) isolated system.
(f) Give relation between $\Delta \mathrm{H}$ and $\Delta \mathrm{E}$ of a reaction.
(g) Indicate in each case whether the entropy of the system would increase or decrease
(i) $\mathrm{H}_{2} \mathrm{O}(l) \rightarrow \mathrm{H}_{2} \mathrm{O}(\mathrm{s})$
(ii) $\mathrm{H}_{2}(300 \mathrm{~K}) \rightarrow \mathrm{H}_{2}(150 \mathrm{~K})$
(iii) $3 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{O}_{3}(\mathrm{~g})$
(iv) $\mathrm{I}_{2}(\mathrm{~g}) \rightarrow \mathrm{I}_{2}$ (s)
(h) Calculate the entropy change for the reaction:

$$
2 \mathrm{H}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)
$$

at 300 K if the standard entropies of $\mathrm{H}_{2}(\mathrm{~g}), \mathrm{O}_{2}(\mathrm{~g})$ and $\mathrm{H}_{2} \mathrm{O}(l)$ are $128.6 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1} .201 .2 \mathrm{JK}^{-}$ ${ }^{1} \mathrm{~mol}^{-1}$ and $68.0 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$ respectively.
(i) What are the characteristics of equilibrium state?
(j) When sulphur in the form $\mathrm{S}_{8}$ is heated at 900 K its initial pressure of 1atm falls by 0.299 at equilibrium. This is because of conversion of some $\mathrm{S}_{8}$ to $\mathrm{S}_{2}$.
$(2 \times 10=20)$
3. (a) Calculate the molar mass of a substance, 0.4 gram of which when dissolved in 29 g benzene lowers its freezing point by $0.75 \mathrm{~K}_{\mathrm{f}}$ for benzene $\left.=5.1 \mathrm{~K} \mathrm{~kg} \mathrm{~mol}^{-1}\right)$
The normal molar mass of the substance is $68 \mathrm{~g} \mathrm{~mol}^{-1}$. What is its molecular state in the solution?
(b) Explain briefly how:
(i) smoke is precipitated.
(ii) rubber is electrolysed.
(c) Calculate the enthalpy of the following reaction

$$
\mathrm{C}_{2} \mathrm{H}_{4}(\mathrm{~g})+\mathrm{HCl}(\mathrm{~g}) \rightarrow \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Cl}(\mathrm{~g})
$$

Given that the bond energies are :

$$
\begin{array}{llll}
\mathrm{C}=\mathrm{C} & 615.1 \mathrm{~kJ} \mathrm{~mol}^{-1} ; & \mathrm{C}=\mathrm{C} & 347.7 \mathrm{~kJ} \mathrm{~mol}^{-1} \\
\mathrm{C}-\mathrm{H} & 413.4 \mathrm{~kJ} \mathrm{~mol}^{-1} ; & \mathrm{H}-\mathrm{Cl} & 431.8 \mathrm{~kJ} \mathrm{~mol}^{-1} \text { and } \\
\mathrm{C}-\mathrm{Cl} & 328.4 \mathrm{~kJ} \mathrm{~mol}^{-1} & &
\end{array}
$$

(d) Calculate the temperature up to which the following reaction would not be spontaneous:

$$
\begin{gathered}
\mathrm{M}_{2} \mathrm{O}(\mathrm{~s}) \rightarrow 2 \mathrm{M}(\mathrm{~s})+\frac{1}{2} \mathrm{O}_{2}(\mathrm{~g}) \\
\Delta \mathrm{H}^{\mathrm{o}}=30 \mathrm{~kJ} \mathrm{~mol}^{-1} \text { and } \Delta \mathrm{S}^{\mathrm{o}}=70 \mathrm{JK}^{-1} \mathrm{~mol}^{-1}
\end{gathered} \quad(3 \times 4=12)
$$

4. (a) $500 \mathrm{~cm}^{3}$ aqueous solution contains 8.0 g of a dibasic acid (molar mass $=80 \mathrm{~g} \mathrm{~mol}^{-1}$ ). The density of the solution is $0.99 \mathrm{~g} \mathrm{~cm}^{-3}$. Calculate molarity, molality and the mole fraction of acid in the solution.
(b) $25 \mathrm{~cm}^{3}$ of $\mathrm{H}_{2}$ and $18 \mathrm{~cm}^{3}$ of $\mathrm{I}_{2}$ vapour were heated in a sealed vessel at $460^{\circ} \mathrm{C}$. At equilibrium $30.8 \mathrm{~cm}^{3}$ of HI was formed. Calculate the degree of dissociation of HI .
$(4 \times 2=8)$
